The 21st Japanese Olympiad in Informatics (JOI 2021/2022)
Spring Training Camp/Qualifying Trial
March 20-23, 2022 (Komaba, Tokyo)
Contest 1 - Misspelling

## Misspelling

Some time ago, President K had a string $S$ of length $N$ consisting of lower case characters. But, he forgot it. He had a dictionary which contains misspellings of several kinds, and he once took a look at the dictionary to check the misspellings of the string $S$. Now, he remembers that the following is true for the string $S$.

- Let $T_{i}(1 \leq i \leq N)$ be the string obtained from $S$ by deleting the $i$-th character and removing the gap. For each $j(1 \leq j \leq M)$, the relation $T_{A_{j}} \leq T_{B_{j}}$ holds.

Here, $T_{A_{j}} \leq T_{B_{j}}$ means either $T_{A_{j}}$ is equal to $T_{B_{j}}$, or $T_{A_{j}}$ is smaller than $T_{B_{j}}$ in the lexicographic order (alphabetical order).

Write a program which, given information on the string $S$ remembered by President K , calculates the number of strings $S$ modulo 1000000007 which do not contradict given information.

## Input

Read the following data from the standard input. Given values are all integers.

$$
\begin{aligned}
& N M \\
& A_{1} B_{1} \\
& A_{2} B_{2} \\
& \vdots \\
& A_{M} B_{M}
\end{aligned}
$$

## Output

Write one line to the standard output. The output should contain the number of strings $S$ modulo 1000000007 which do not contradict given information.

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## Constraints

- $2 \leq N \leq 500000$.
- $1 \leq M \leq 500000$.
- $1 \leq A_{j} \leq N(1 \leq j \leq M)$.
- $1 \leq B_{j} \leq N(1 \leq j \leq M)$.
- $A_{j} \neq B_{j}(1 \leq j \leq M)$.
- $\left(A_{j}, B_{j}\right) \neq\left(A_{k}, B_{k}\right)(1 \leq j<k \leq M)$.


## Subtasks

1. (8 points) $N \leq 10$.
2. (20 points) $N \leq 200$.
3. (29 points) $M=N-1$. Moreover, there exists a permutation $P$ of $(1,2, \ldots, N)$ of length $N$ satisfying $A_{j}=P_{j}$ and $B_{j}=P_{j+1}(1 \leq j \leq M)$.
4. (32 points) $N \leq 20000$.
5. (11 points) No additional constraints.

## Sample Input and Output

| Sample Input 1 | Sample Output 1 |
| :--- | :--- |
| 3 | 2 |
| 1 | 3 |
| 3 | 2 |

For example, if the string $S$ is bab, we have $T_{1}=\mathrm{ab}, T_{2}=\mathrm{bb}, T_{3}=\mathrm{ba}$. The relations $T_{1} \leq T_{3}$ and $T_{3} \leq T_{2}$ hold. This string does not contradict given information. In total, there are 5876 strings $S$ which do not contradict given information. Therefore, output 5876.

On the other hand, for example, if the strings $S$ is aab, we have $T_{1}=\mathrm{ab}, T_{2}=\mathrm{ab}, T_{3}=\mathrm{aa}$. The relation $T_{1} \leq T_{3}$ does not hold. Therefore, this string contradicts given information.

This sample input satisfies the constraints of all the subtasks.

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| Sample Input 2 | Sample Output 2 |
| :--- | :--- |
| 5 | 6 |
| 1 | 2 |
| 1 | 5 |
| 2 | 4 |
| 5 | 4 |
| 5 | 3 |
| 4 | 3 |

This sample input satisfies the constraints of Subtasks $1,2,4,5$.
$\left.\begin{array}{|l|l|}\hline \text { Sample Input 3 } & \text { Sample Output 3 } \\ \hline 10 & 9 \\ 3 & 6 \\ 4 & 6 \\ 6 & 7 \\ 7 & 9 \\ 10 & 8 \\ 9 & 8 \\ 8 & 5 \\ 5 & 2 \\ 5 & 1\end{array}\right]$

The number of strings $S$ which do not contradict given information is 824206295601 . Therefore, output 206289833 , which is the remainder of 824206295601 when divided by 1000000007.

This sample input satisfies the constraints of Subtasks 1, 2, 4, 5 .

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$\left.\begin{array}{|l|l|}\hline \text { Sample Input 4 } & \text { Sample Output 4 } \\ \hline 7 & 6 \\ 1 & 3 \\ 3 & 4 \\ 4 & 6 \\ 6 & 5 \\ 5 & 7 \\ 7 & 2\end{array}\right]$

This sample input satisfies the constraints of all the subtasks.

| Sample Input 5 | Sample Output 5 |
| :--- | :--- |
| 5 | 4 |
| 2 | 4 |
| 4 | 3 |
| 3 | 5 |
| 5 | 1 |

This sample input satisfies the constraints of all the subtasks.

